

Na₉Pb₄ (δ' -NaPb) Structure: A9B4_hP26_194_ce3f_ef-001

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<https://aflow.org/prototype-encyclopedia/J5ST>

https://aflow.org/prototype-encyclopedia/A9B4_hP26_194_ce3f_ef-001

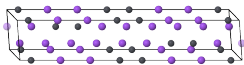
Prototype	Na ₉ Pb ₄
AFLOW prototype label	A9B4_hP26_194_ce3f_ef-001
Pearson symbol	hP26
Space group number	194
Space group symbol	$P6_3/mmc$
AFLOW prototype command	<code>aflow --proto=A9B4_hP26_194_ce3f_ef-001</code> <code>--params=a, c/a, z₂, z₃, z₄, z₅, z₆, z₇</code>

- (Weston, 1957) determined the space group, lattice constants, and positions of the lead atoms in Na₉Pb₄ but were unable to place the sodium atoms. Using the First-Principles Assisted Structure Solution (FPASS) method, (Ward, 2015) determined a set of positions for the sodium atoms consistent with the available experimental data. To our knowledge further experimental study of Na₉Pb₄ has taken place.
- We have shifted the origin of the $\hat{z}$ axis by $c/2$ from that chosen by (Weston, 1957), changing the Na-I site from the (2d) Wyckoff position to (2c).
- There is no ICSD entry for this structure, but (Ward, 2015) provide the CIF for this structure in their supplementary material.

Hexagonal primitive vectors

$$\begin{aligned} \mathbf{a}_1 &= \frac{1}{2}a\hat{x} - \frac{\sqrt{3}}{2}a\hat{y} \\ \mathbf{a}_2 &= \frac{1}{2}a\hat{x} + \frac{\sqrt{3}}{2}a\hat{y} \\ \mathbf{a}_3 &= c\hat{z} \end{aligned}$$

$\begin{matrix} \textcolor{red}{a_1} \\ \textcolor{blue}{a_2} \\ \textcolor{red}{a_3} \end{matrix}$



Basis vectors

Lattice coordinates	Cartesian coordinates	Wyckoff position	Atom type
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$\mathbf{B}_1$	$=$	$\frac{1}{3} \mathbf{a}_1 + \frac{2}{3} \mathbf{a}_2 + \frac{1}{4} \mathbf{a}_3$	$=$	$\frac{1}{2} a \hat{\mathbf{x}} + \frac{\sqrt{3}}{6} a \hat{\mathbf{y}} + \frac{1}{4} c \hat{\mathbf{z}}$	(2c)	Na I
$\mathbf{B}_2$	$=$	$\frac{2}{3} \mathbf{a}_1 + \frac{1}{3} \mathbf{a}_2 + \frac{3}{4} \mathbf{a}_3$	$=$	$\frac{1}{2} a \hat{\mathbf{x}} - \frac{\sqrt{3}}{6} a \hat{\mathbf{y}} + \frac{3}{4} c \hat{\mathbf{z}}$	(2c)	Na I
$\mathbf{B}_3$	$=$	$z_2 \mathbf{a}_3$	$=$	$c z_2 \hat{\mathbf{z}}$	(4e)	Na II
$\mathbf{B}_4$	$=$	$(z_2 + \frac{1}{2}) \mathbf{a}_3$	$=$	$c (z_2 + \frac{1}{2}) \hat{\mathbf{z}}$	(4e)	Na II
$\mathbf{B}_5$	$=$	$-z_2 \mathbf{a}_3$	$=$	$-c z_2 \hat{\mathbf{z}}$	(4e)	Na II
$\mathbf{B}_6$	$=$	$-(z_2 - \frac{1}{2}) \mathbf{a}_3$	$=$	$-c (z_2 - \frac{1}{2}) \hat{\mathbf{z}}$	(4e)	Na II
$\mathbf{B}_7$	$=$	$z_3 \mathbf{a}_3$	$=$	$c z_3 \hat{\mathbf{z}}$	(4e)	Pb I
$\mathbf{B}_8$	$=$	$(z_3 + \frac{1}{2}) \mathbf{a}_3$	$=$	$c (z_3 + \frac{1}{2}) \hat{\mathbf{z}}$	(4e)	Pb I
$\mathbf{B}_9$	$=$	$-z_3 \mathbf{a}_3$	$=$	$-c z_3 \hat{\mathbf{z}}$	(4e)	Pb I
$\mathbf{B}_{10}$	$=$	$-(z_3 - \frac{1}{2}) \mathbf{a}_3$	$=$	$-c (z_3 - \frac{1}{2}) \hat{\mathbf{z}}$	(4e)	Pb I
$\mathbf{B}_{11}$	$=$	$\frac{1}{3} \mathbf{a}_1 + \frac{2}{3} \mathbf{a}_2 + z_4 \mathbf{a}_3$	$=$	$\frac{1}{2} a \hat{\mathbf{x}} + \frac{\sqrt{3}}{6} a \hat{\mathbf{y}} + c z_4 \hat{\mathbf{z}}$	(4f)	Na III
$\mathbf{B}_{12}$	$=$	$\frac{2}{3} \mathbf{a}_1 + \frac{1}{3} \mathbf{a}_2 + (z_4 + \frac{1}{2}) \mathbf{a}_3$	$=$	$\frac{1}{2} a \hat{\mathbf{x}} - \frac{\sqrt{3}}{6} a \hat{\mathbf{y}} + c (z_4 + \frac{1}{2}) \hat{\mathbf{z}}$	(4f)	Na III
$\mathbf{B}_{13}$	$=$	$\frac{2}{3} \mathbf{a}_1 + \frac{1}{3} \mathbf{a}_2 - z_4 \mathbf{a}_3$	$=$	$\frac{1}{2} a \hat{\mathbf{x}} - \frac{\sqrt{3}}{6} a \hat{\mathbf{y}} - c z_4 \hat{\mathbf{z}}$	(4f)	Na III
$\mathbf{B}_{14}$	$=$	$\frac{1}{3} \mathbf{a}_1 + \frac{2}{3} \mathbf{a}_2 - (z_4 - \frac{1}{2}) \mathbf{a}_3$	$=$	$\frac{1}{2} a \hat{\mathbf{x}} + \frac{\sqrt{3}}{6} a \hat{\mathbf{y}} - c (z_4 - \frac{1}{2}) \hat{\mathbf{z}}$	(4f)	Na III
$\mathbf{B}_{15}$	$=$	$\frac{1}{3} \mathbf{a}_1 + \frac{2}{3} \mathbf{a}_2 + z_5 \mathbf{a}_3$	$=$	$\frac{1}{2} a \hat{\mathbf{x}} + \frac{\sqrt{3}}{6} a \hat{\mathbf{y}} + c z_5 \hat{\mathbf{z}}$	(4f)	Na IV
$\mathbf{B}_{16}$	$=$	$\frac{2}{3} \mathbf{a}_1 + \frac{1}{3} \mathbf{a}_2 + (z_5 + \frac{1}{2}) \mathbf{a}_3$	$=$	$\frac{1}{2} a \hat{\mathbf{x}} - \frac{\sqrt{3}}{6} a \hat{\mathbf{y}} + c (z_5 + \frac{1}{2}) \hat{\mathbf{z}}$	(4f)	Na IV
$\mathbf{B}_{17}$	$=$	$\frac{2}{3} \mathbf{a}_1 + \frac{1}{3} \mathbf{a}_2 - z_5 \mathbf{a}_3$	$=$	$\frac{1}{2} a \hat{\mathbf{x}} - \frac{\sqrt{3}}{6} a \hat{\mathbf{y}} - c z_5 \hat{\mathbf{z}}$	(4f)	Na IV
$\mathbf{B}_{18}$	$=$	$\frac{1}{3} \mathbf{a}_1 + \frac{2}{3} \mathbf{a}_2 - (z_5 - \frac{1}{2}) \mathbf{a}_3$	$=$	$\frac{1}{2} a \hat{\mathbf{x}} + \frac{\sqrt{3}}{6} a \hat{\mathbf{y}} - c (z_5 - \frac{1}{2}) \hat{\mathbf{z}}$	(4f)	Na IV
$\mathbf{B}_{19}$	$=$	$\frac{1}{3} \mathbf{a}_1 + \frac{2}{3} \mathbf{a}_2 + z_6 \mathbf{a}_3$	$=$	$\frac{1}{2} a \hat{\mathbf{x}} + \frac{\sqrt{3}}{6} a \hat{\mathbf{y}} + c z_6 \hat{\mathbf{z}}$	(4f)	Na V
$\mathbf{B}_{20}$	$=$	$\frac{2}{3} \mathbf{a}_1 + \frac{1}{3} \mathbf{a}_2 + (z_6 + \frac{1}{2}) \mathbf{a}_3$	$=$	$\frac{1}{2} a \hat{\mathbf{x}} - \frac{\sqrt{3}}{6} a \hat{\mathbf{y}} + c (z_6 + \frac{1}{2}) \hat{\mathbf{z}}$	(4f)	Na V
$\mathbf{B}_{21}$	$=$	$\frac{2}{3} \mathbf{a}_1 + \frac{1}{3} \mathbf{a}_2 - z_6 \mathbf{a}_3$	$=$	$\frac{1}{2} a \hat{\mathbf{x}} - \frac{\sqrt{3}}{6} a \hat{\mathbf{y}} - c z_6 \hat{\mathbf{z}}$	(4f)	Na V
$\mathbf{B}_{22}$	$=$	$\frac{1}{3} \mathbf{a}_1 + \frac{2}{3} \mathbf{a}_2 - (z_6 - \frac{1}{2}) \mathbf{a}_3$	$=$	$\frac{1}{2} a \hat{\mathbf{x}} + \frac{\sqrt{3}}{6} a \hat{\mathbf{y}} - c (z_6 - \frac{1}{2}) \hat{\mathbf{z}}$	(4f)	Na V
$\mathbf{B}_{23}$	$=$	$\frac{1}{3} \mathbf{a}_1 + \frac{2}{3} \mathbf{a}_2 + z_7 \mathbf{a}_3$	$=$	$\frac{1}{2} a \hat{\mathbf{x}} + \frac{\sqrt{3}}{6} a \hat{\mathbf{y}} + c z_7 \hat{\mathbf{z}}$	(4f)	Pb II
$\mathbf{B}_{24}$	$=$	$\frac{2}{3} \mathbf{a}_1 + \frac{1}{3} \mathbf{a}_2 + (z_7 + \frac{1}{2}) \mathbf{a}_3$	$=$	$\frac{1}{2} a \hat{\mathbf{x}} - \frac{\sqrt{3}}{6} a \hat{\mathbf{y}} + c (z_7 + \frac{1}{2}) \hat{\mathbf{z}}$	(4f)	Pb II
$\mathbf{B}_{25}$	$=$	$\frac{2}{3} \mathbf{a}_1 + \frac{1}{3} \mathbf{a}_2 - z_7 \mathbf{a}_3$	$=$	$\frac{1}{2} a \hat{\mathbf{x}} - \frac{\sqrt{3}}{6} a \hat{\mathbf{y}} - c z_7 \hat{\mathbf{z}}$	(4f)	Pb II
$\mathbf{B}_{26}$	$=$	$\frac{1}{3} \mathbf{a}_1 + \frac{2}{3} \mathbf{a}_2 - (z_7 - \frac{1}{2}) \mathbf{a}_3$	$=$	$\frac{1}{2} a \hat{\mathbf{x}} + \frac{\sqrt{3}}{6} a \hat{\mathbf{y}} - c (z_7 - \frac{1}{2}) \hat{\mathbf{z}}$	(4f)	Pb II

References

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- [2] N. E. Weston and D. P. Shoemaker, *The crystal structures of three phases in the Na-Pb system*, Acta Cryst. **10**, 775 (1957), doi:10.1107/S0365110X57002649. International Union of Crystallography Abstracts, pp. 735-863.

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Na
Pb

