

Corundum (α -alumina, Al_2O_3 , $D5_1$) Structure: A2B3_hR10_167_c-e-001

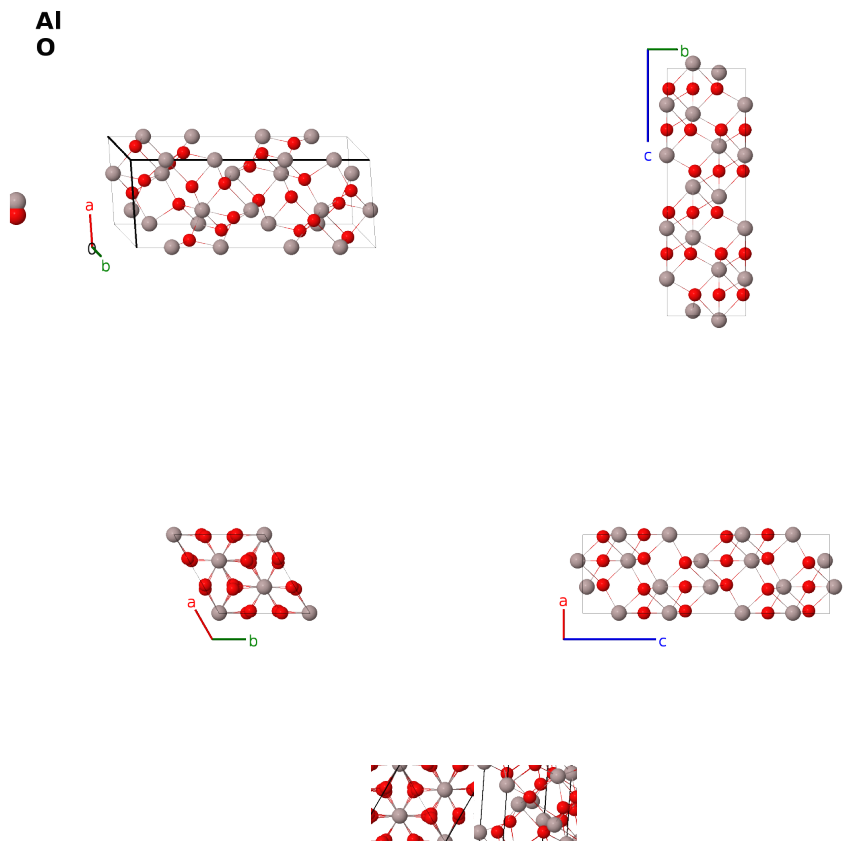
This structure previously used the label(s) **A2B3_hR10_167_c-e**. Calls to these addresses will be redirected here.

Cite this page as:

- H. Eckert, S. Divilov, M. J. Mehl, D. Hicks, A. C. Zettel, M. Esters, X. Campilongo, and S. Curtarolo, *The AFLOW Library of Crystallographic Prototypes: Part 4*, Comput. Mater. Sci. **240**, 112988 (2024), doi: 10.1016/j.commatsci.2024.112988.
- D. Hicks, M. J. Mehl, M. Esters, C. Oses, O. Levy, G. L. W. Hart, C. Toher, and S. Curtarolo, *The AFLOW Library of Crystallographic Prototypes: Part 3*, Comput. Mater. Sci. **199**, 110450 (2021), doi: 10.1016/j.commatsci.2021.110450.

<https://aflow.org/prototype-encyclopedia/CBQY>

https://aflow.org/prototype-encyclopedia/A2B3_hR10_167_c-e-001



Prototype	Al_2O_3
AFLOW prototype label	A2B3_hR10_167_c-e-001
<i>Strukturbericht</i> designation	$D5_1$
Mineral name	corundum
ICSD	9770
CCDC	1594710
Pearson symbol	hR10
Space group number	167

Space group symbol	$R\bar{3}c$
AFLOW prototype command	afLOW --proto=A2B3_hR10_167_c_e-001 --params=a, c/a, x ₁ , x ₂

Other compounds with this structure

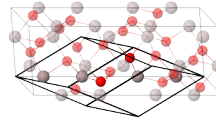
γ -Al₂S₃, Co₂O₃, Cr₂O₃ (eskolait), Fe₂O₃ (hematite), (Fe, Ge)₂O₃, α -Ga₂O₃, In₂O₃, In₂S₃, (In, V)₂O₃, Lu₂S₃, (Mn, Sn)₂O₃, N₂Ca₃, Rh₂O₃, Ru₂C₃, Sc₂O₃, Ti₂O₃ (tistarite), Tm₂S₃, V₂O₃, Yb₂S₃, Lu₂S₃, Rh₂O₃, V₂O₃ (karelianite), Yb₂S₃

- Alumina comes in a variety of forms. In the Encyclopedia we have:
 - Corundum, or α -alumina ($D5_1$) (this structure) is the mineral usual found in nature.
 - β -alumina ($D5_6$)
 - We describe γ -alumina ($D5_7$) using Fe₂O₃ as the prototype.
 - δ -alumina is a tetragonal distortion of the spinel structure. It is found in nature as deltalumite.
 - κ -Al₂O₃.
- In corundum the aluminum atoms can be replaced by two different species of atoms stacked in alternating layers along the c -axis, forming the ilmenite structure.
- Alloying with Fe and Ti produces sapphire (a blue crystal), and alloying with Cr produces ruby (a red crystal).
- Hexagonal settings of rhombohedral structures can be obtained with the option **--hex**.

Rhombohedral primitive vectors

$$\begin{aligned}
 \mathbf{a}_1 &= \frac{1}{2}a \hat{\mathbf{x}} - \frac{\sqrt{3}}{6}a \hat{\mathbf{y}} + \frac{1}{3}c \hat{\mathbf{z}} \\
 \mathbf{a}_2 &= \frac{1}{\sqrt{3}}a \hat{\mathbf{y}} + \frac{1}{3}c \hat{\mathbf{z}} \\
 \mathbf{a}_3 &= -\frac{1}{2}a \hat{\mathbf{x}} - \frac{\sqrt{3}}{6}a \hat{\mathbf{y}} + \frac{1}{3}c \hat{\mathbf{z}}
 \end{aligned}$$

$\begin{matrix} \textcolor{red}{a}_1 \\ \textcolor{blue}{a}_2 \end{matrix}$



Basis vectors

	Lattice coordinates		Cartesian coordinates	Wyckoff position	Atom type
$\mathbf{B}_1$	$= x_1 \mathbf{a}_1 + x_1 \mathbf{a}_2 + x_1 \mathbf{a}_3$	$=$	$cx_1 \hat{\mathbf{z}}$	(4c)	Al I
$\mathbf{B}_2$	$= -\left(x_1 - \frac{1}{2}\right) \mathbf{a}_1 - \left(x_1 - \frac{1}{2}\right) \mathbf{a}_2 - \left(x_1 - \frac{1}{2}\right) \mathbf{a}_3$	$=$	$-c\left(x_1 - \frac{1}{2}\right) \hat{\mathbf{z}}$	(4c)	Al I
$\mathbf{B}_3$	$= -x_1 \mathbf{a}_1 - x_1 \mathbf{a}_2 - x_1 \mathbf{a}_3$	$=$	$-cx_1 \hat{\mathbf{z}}$	(4c)	Al I
$\mathbf{B}_4$	$= \left(x_1 + \frac{1}{2}\right) \mathbf{a}_1 + \left(x_1 + \frac{1}{2}\right) \mathbf{a}_2 + \left(x_1 + \frac{1}{2}\right) \mathbf{a}_3$	$=$	$c\left(x_1 + \frac{1}{2}\right) \hat{\mathbf{z}}$	(4c)	Al I
$\mathbf{B}_5$	$= x_2 \mathbf{a}_1 - \left(x_2 - \frac{1}{2}\right) \mathbf{a}_2 + \frac{1}{4} \mathbf{a}_3$	$=$	$\frac{1}{8}a(4x_2 - 1) \hat{\mathbf{x}} - \frac{\sqrt{3}}{8}a(4x_2 - 1) \hat{\mathbf{y}} + \frac{1}{4}c \hat{\mathbf{z}}$	(6e)	O I
$\mathbf{B}_6$	$= \frac{1}{4} \mathbf{a}_1 + x_2 \mathbf{a}_2 - \left(x_2 - \frac{1}{2}\right) \mathbf{a}_3$	$=$	$\frac{1}{8}a(4x_2 - 1) \hat{\mathbf{x}} + \frac{\sqrt{3}}{8}a(4x_2 - 1) \hat{\mathbf{y}} + \frac{1}{4}c \hat{\mathbf{z}}$	(6e)	O I
$\mathbf{B}_7$	$= -\left(x_2 - \frac{1}{2}\right) \mathbf{a}_1 + \frac{1}{4} \mathbf{a}_2 + x_2 \mathbf{a}_3$	$=$	$-a\left(x_2 - \frac{1}{4}\right) \hat{\mathbf{x}} + \frac{1}{4}c \hat{\mathbf{z}}$	(6e)	O I
$\mathbf{B}_8$	$= -x_2 \mathbf{a}_1 + \left(x_2 + \frac{1}{2}\right) \mathbf{a}_2 + \frac{3}{4} \mathbf{a}_3$	$=$	$-\frac{1}{8}a(4x_2 + 3) \hat{\mathbf{x}} + \frac{\sqrt{3}}{24}a(12x_2 + 1) \hat{\mathbf{y}} + \frac{5}{12}c \hat{\mathbf{z}}$	(6e)	O I
$\mathbf{B}_9$	$= \frac{3}{4} \mathbf{a}_1 - x_2 \mathbf{a}_2 + \left(x_2 + \frac{1}{2}\right) \mathbf{a}_3$	$=$	$-\frac{1}{8}a(4x_2 - 1) \hat{\mathbf{x}} - \frac{\sqrt{3}}{24}a(12x_2 + 5) \hat{\mathbf{y}} + \frac{5}{12}c \hat{\mathbf{z}}$	(6e)	O I

$$\mathbf{B}_{10} = \left(x_2 + \frac{1}{2}\right) \mathbf{a}_1 + \frac{3}{4} \mathbf{a}_2 - x_2 \mathbf{a}_3 = a \left(x_2 + \frac{1}{4}\right) \hat{\mathbf{x}} + \frac{\sqrt{3}}{6} a \hat{\mathbf{y}} + \frac{5}{12} c \hat{\mathbf{z}} \quad (6e) \quad \text{O I}$$

References

- [1] L. W. Finger and R. M. Hazen, *Crystal structure and compression of ruby to 46 kbar*, J. Appl. Phys. **49**, 5823–5826 (1978), doi:10.1063/1.324598.

First cited in

M. J. Mehl, D. Hicks, C. Toher, O. Levy, R. M. Hanson, G. L. W. Hart, and S. Curtarolo, *The AFLOW Library of Crystallographic Prototypes: Part 1*, Comput. Mater. Sci. **136**, S1-828 (2017). doi: 10.1016/j.commatsci.2017.01.017